

Automatic detection of cereal rows by means of pattern recognition techniques

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Abstract

Automatic locating of weeds from fields is an active research topic in precision agriculture. A reliable and practical plant identification technique would enable the reduction of herbicide amounts and lowering of production costs, along with reducing the damage to the ecosystem. When the seeds have been sown row-wise, most weeds may be located between the sowing rows. The present work describes a clustering-based method for recognition of plantlet rows from a set of aerial photographs, taken by a drone flying at approximately ten meters. The algorithm includes three phases: segmentation of green objects in the view, feature extraction, and clustering of plants into individual rows. Segmentation separates the plants from the background. The main feature to be extracted is the center of gravity of each plant segment. A tentative clustering is obtained piecewise by applying the 2D Fourier transform to image blocks to get information about the direction and the distance between the rows. The precise sowing line position is finally derived by principal component analysis. The method was able to find the rows from a set of photographs of size 1452×969 pixels approximately in 0.11 seconds, with the accuracy of 94 per cent.

Keywords: computer vision, pattern recognition, principal component analysis, Fourier transform, precision agriculture

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1. Introduction

Machine vision, based on imaging by satellites, aeroplanes or drones, is a central research field in precision agriculture. Due to getting cheaper and more versatile, drones have quickly gained popularity in precision agriculture. Images taken from low-flying drones are in many cases precise enough for inspection of individual plants – something not reachable by the means of satellites (Maes and Steppe, 2018).

There have been prior projects for estimating the number, height, and locations of individual plants (see for example Sogaard and Olsen 2003; Tang and Tian 2005; Bakker et al. 2008a; Bakker et al. 2008b; Jiang et al. 2015). The health of plants, as well as the existence and location of weeds are also important issues to be observed (Woebbecke et al., 1995; Southall et al., 2002; Burgos-Artizzu et al., 2011). Traditional farm machines or more modern robots (usually on wheels) can be used to locally spray nutrients on small areas, or herbicides on the detected weeds. By local application of herbicides, reductions between 4 to 94 per cent in the herbicide amounts have been obtained in field experiments (de Castro et al., 2012, 2013).

The aim of the present study was to design novel methods for early detection of monocot weeds between cereal rows. Monocot weeds cannot easily be distinguished from the cereals by form or color, and their identification is possible only at a later stage when it may be too late for weed removal operations. We are particularly interested in common wild oat (*Avena fatua* L), a weed widely infesting cereals in Europe.

Early detection of monocot weeds can be based on the fact that cereals are sown in regular rows whereas most weeds would not grow within the rows. For weed detection, automatic classification of each plant in a field photograph to either a plantlet growing in a row or a plant growing in-between the rows will help to detect most weeds and to identify weed-infested areas. In the present study, we took the first step toward identifying plants growing in rows and between rows by developing a method for locating the rows in drone photographs

31 taken from a weedless field.

32 **2. Previous research**

33 Research on methods for the detection of crop rows has focused on guiding
34 of a tractor or an agricultural robot along the crop rows. For this reason, images
35 used for row detection have typically been taken from an altitude of maximally
36 two meters and show only few crop rows that run from the bottom of the picture
37 to the top with a strong perspective (Marchant and Brivot 1995; Kise et al. 2005;
38 Bossu et al. 2009; Anter et al. 2019; Jiang et al. 2015; Jiang et al. 2016; Zhang
39 et al. 2018). Furthermore, the tested agricultural settings have been mostly
40 limited to conditions in which such robotic devices are feasible, and therefore
41 relatively large plants with a clear row structure like cauliflower (Marchant and
42 Brivot, 1995), maize (Zhang et al., 2018), soybean (Kise et al., 2005), sugar beet,
43 canola (Winterhalter et al., 2018) and potato (Vidović et al., 2016), or plants
44 with dense rows (Jiang et al., 2016) or large row spacing like in paddy rice (Choi
45 et al., 2015) have been tested. The methods are designed to function in real-
46 time, and therefore low-resolution pictures are often preferred, from 3000x2250
47 (García-Santillín et al., 2018) down to 320x240 resolution (Vidović et al., 2016).
48 The most common camera system has been a standard RGB camera, although
49 also NIR cameras (Kise et al. 2005; Choi et al. 2015) and stereo vision or laser
50 scanning (Winterhalter et al., 2018) have been used.

51 Several computational methods have been applied to row detection. All
52 these methods need knowledge about the positions of the plant pixels. In RGB
53 photographs, the plant/soil discrimination is usually done by calculating the
54 greenness of a pixel by a vegetation index (e.g. Woebbecke et al. 1995, Motohka
55 et al. 2010, Burgos-Artizzu et al. 2011, and Jiang et al. 2015) and refined with
56 thresholding with Otsu’s method (Otsu, 1975) or by k-means clustering (Han
57 et al., 2004). Søgaard and Olsen (2003) avoid the segmentation step in their row
58 recognizer. They convert the colour image into gray-scale by a linear transform
59 emphasizing the green channel. After plant/soil separation, methods detecting

60 individual plants often calculate a single point defining the position of the plant;
61 methods used for this task depend strongly on the plant species. For example,
62 the horizontal center of an individual paddy rice plant is a well-defined concept
63 when the plant is visible in a low-altitude picture taken from an inclined position
64 (Choi et al., 2015).

65 The simplest methods designed for the purpose of guiding a vehicle are
66 based on the idea that the distribution of plant pixels in a horizontal slice of
67 the photograph concentrates on the rows (Reid and Searcy 1987; Olsen 1995;
68 Søggaard and Olsen 2003). These methods work best when the areas between
69 plant rows are homogeneous, i.e. free of weeds. In addition, rows with sparsely
70 growing plants will cause difficulties for these methods. The crop row detection
71 methods have been refined with the idea that in a perspective picture, the rows
72 point to a common vanishing point (Pla et al. 1997; Jiang et al. 2016). These
73 methods function only for pictures in which the rows run approximately from
74 bottom to top but they have the advantage of not being dependent on any
75 specific method of defining the center of an individual plant.

76 A more advanced method that has extensively been applied to row detection
77 is Hough transform that uses a voting scheme to detect line segments in pictures
78 (Marchant and Brivot 1995; Bakker et al. 2008a; Choi et al. 2015; Jiang et al.
79 2016; García-Santillín et al. 2018). The Hough transform is generally quite
80 slow, which restricts its utilization in real-time detection. The computing time
81 can be decreased by first defining the plant center (Choi et al., 2015). The
82 Hough transform can detect rows of any direction in the image, but if the rows
83 have gaps or there are weeds in the picture, the Hough transform may detect
84 additional lines that are not parallel with the crop rows (Marchant and Brivot
85 1995; Choi et al. 2015). Therefore the results need to be refined after the initial
86 Hough transform. Application of the wavelet transform for row detection has
87 given relatively long computation times (Bossu et al., 2009).

88 The third method commonly used for row detection is linear regression
89 (Billingsley and Schoenfisch 1997; Søggaard and Olsen 2003; Han et al. 2004;
90 Jiang et al. 2015). In this method, the picture can be divided to windows

91 around each candidate point, and candidate crop rows are obtained by calculat-
92 ing linear regression of the candidate points inside each separate windows. The
93 validity of each regression line is then assessed e.g. by calculating the moment of
94 inertia of the pixels of the window with regard to the candidate row (Billingsley
95 and Schoenfisch 1997; Jiang et al. 2015). García-Santillín et al. (2018) applied
96 curvilinear regression models in combination with the Hough transform for de-
97 tection of curved rows. Linear regression does not depend on the row directions
98 but would lead to a very large number of candidate rows in a picture taken from
99 above of a field, with large gaps in rows.

100 Recent research on row detection methods has led to suggestions for global
101 fitting methods that seek to avoid errors caused by gaps, weeds, plant morphol-
102 ogy and local or global curvature of rows. These methods include the global
103 energy minimization method of Vidović et al. (2016) that looks for regular pat-
104 terns and the pattern Hough transform method for simultaneous detection of all
105 rows and row spacing (Winterhalter et al., 2018). The use of 3D imaging (Win-
106 terhalter et al., 2018) is another potential future method, as the laser scanning
107 technique develops rapidly.

108 In the present study, the photographs were taken from a moderate altitude
109 from above the field. Therefore many of the previous methods for row detection
110 are not directly applicable to our case. In the method of Jiang et al. (2015),
111 the colour image is initially segmented by transforming it first into a gray-scale
112 image on the basis of a vegetation index (Burgos-Artizzu et al., 2011). The
113 gray-scale image is then binarized, by using a threshold given by the method
114 of Otsu (1975). In the second phase, the center points of the seed rows will
115 be determined by solving an optimization problem that assumes a constant
116 distance between adjacent rows. The solution produces both real and erroneous
117 center points. The latter ones will be filtered using a classification algorithm.
118 The seed rows are finally localized by the least squares method. The approach is
119 promising, and we therefore started our work by applying it to our image data.
120 It turned out that our implementation of the method, with certain carefully
121 selected parameter values and images of certain particular directions of seed

122 rows, produced excellent results (Figs. 1a and 1b).

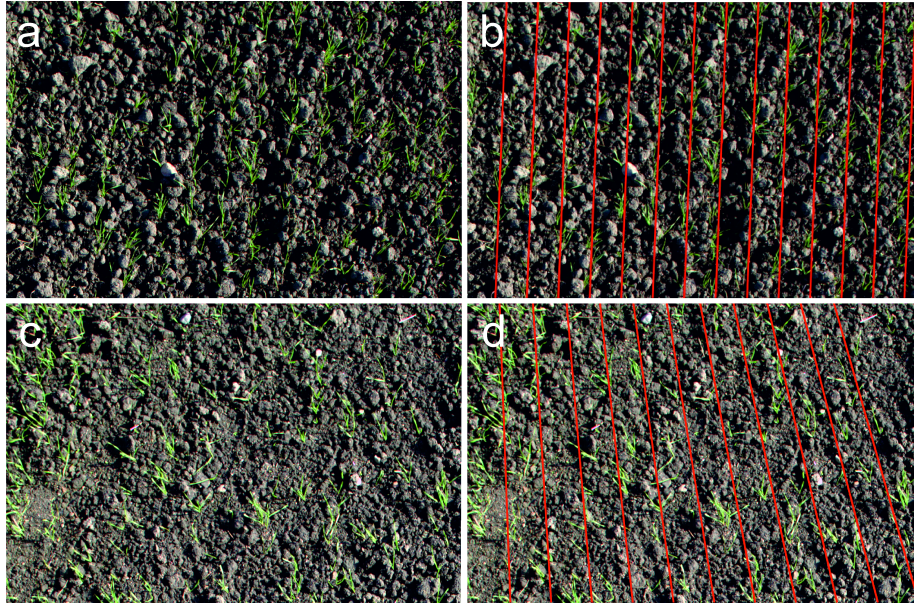


Figure 1: Recognition of seed rows by the method of (Jiang et al., 2015)

123 As a drawback, the method of Jiang et al. (2015) cannot be directly applied
124 if the seed rows are horizontal. The method also tends to fail when the initial
125 center points of rows should be searched in regions with sparse occurrences of
126 plants (Figs. 1c and 1d). The reason for this is that the scanning of the first
127 row is crucial for the success of the whole recognition process, as the remaining
128 center points will be found in relation to this line.

129 Another approach was to apply Hough transform to the binarized image
130 data. As mentioned before, large gaps in the rows cause the method to detect
131 additional lines that do not match the rows. One way to overcome this prob-
132 lem is to restrict the parameter space by searching only lines that are in the
133 same direction as the sowing rows and within the allowed distance from each
134 other. The directional angle θ of the rows can be estimated automatically (to
135 be described in Section 4). Other parameters are predefined, such as minimum
136 line length, a distance between adjacent rows and the minimum value to be

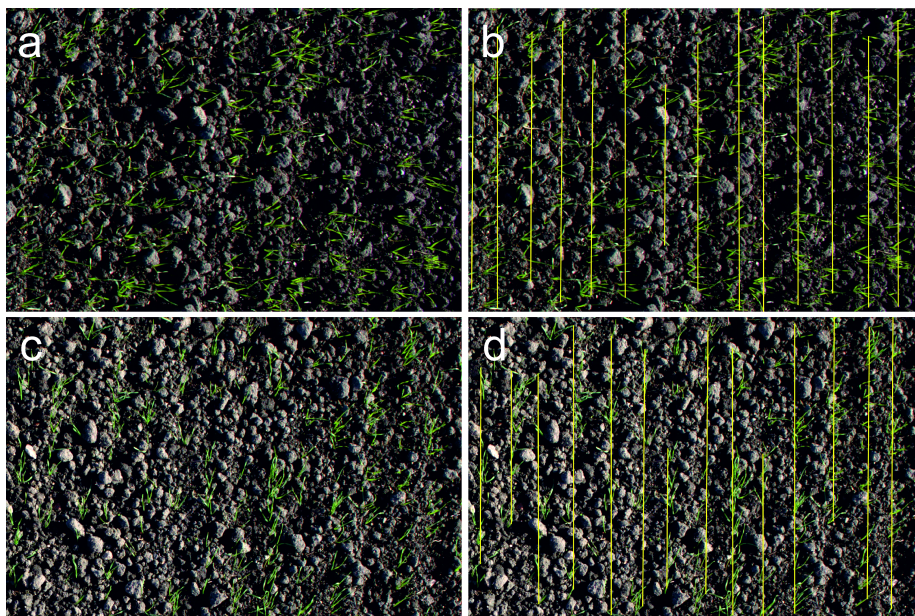


Figure 2: Recognition of seed rows by Hough transform combined with automatic detection of direction of the rows.

137 considered as a peak in the the accumulator space.

138 By tuning these parameters, the method is capable of producing good re-
139 sults (Figs 2a and 2b). However, rows with sparsely growing plants cannot be
140 completely detected (Figs 2c and 2d) and the performance is sensitive to seven
141 handcrafted parameters, which limits its application.

142 The row recognition algorithm used in the present study is based on cluster-
143 ing of plants into rows. We took photographs of a rye field when the shoots of
144 the cereal were about 2-7 centimeters high and the overlap between individual
145 rye plantlets was modest. The algorithm includes two main steps: segmenta-
146 tion of plant areas from the background (soil, stones, shadows, etc.), and their
147 assignment to row clusters. We suggest two alternative algorithms for plant
148 segmentation; *k-means clustering*, and a method that utilizes a transform of the
149 colour channel values, combined with *Otsu's method* (Otsu, 1975). The k-means
150 method turned out to be accurate, but unfortunately rather slow. An alterna-

151 tive *color channel transformation method* was significantly faster, but required
152 more image processing steps.

153 3. Problem setting

154 We are given a set of colour photographs taken by a drone which scans a
155 crop field at the flying height of approximately 10 meters. The task is to design
156 and implement a method which

- 157 (a) separates the individual plants from the background,
- 158 (b) localizes the areas of the image containing the rows of plants,
- 159 (c) allows gaps in the rows, to a certain extent.

160 Unlike the works of Tang and Tian (2005), Southall et al. (2002), Bakker et al.
161 (2008a), and Jiang et al. (2015), the demand for real-time operation of the
162 technique is relaxed. Note that the mentioned earlier approaches are for ap-
163 plications where the photos are supposed to be taken from a moving tractor,
164 coupled with spraying the herbicides, whereas in our case a drone is doing only
165 the data collection for aiding later operation of a weed removal device.

It is assumed that the rows can be modelled as straight lines of the form

$$(x, y) = (\alpha + \beta y, y), \quad (1)$$

166 where β is the slope of the line. The equation allows the description of
167 both inclined lines and those parallel to the y axis. For practical purposes,
168 it is advisable that the drone does not significantly change its orientation with
169 respect to the underlying surface, and the shooting direction of photos is vertical,
170 i.e. the y-axis of the camera approximately parallels with the moving direction
171 of the drone. This is not mandatory for our row detection method, but helps in
172 systematic covering of the field. The need for perspective correction is avoided
173 by dividing the images into sufficiently small windows, within which the row
174 detection is applied separately. In practice, the seed rows consist of groups of
175 parallel rows, where each group corresponds to an array of feeders in the sowing

176 machine. Within groups, the distances between adjacent rows are more or less
177 the same, but between groups, they may vary, due to the possible overlap or gaps
178 between the driving lanes of the sowing machine. In this paper we concentrate
179 on the intra-group modelling, but discuss the options for handling the general
180 case in the conclusions.

181 On a coarse level the proposed row recognizer consists of three main phases;
182 segmentation, feature extraction, and clustering. In segmentation, the plants
183 are separated from the background. After this, they are clustered into disjoint
184 rows, which are finally modelled by the least squares method.

185 **4. Row recognizer**

186 The row recognizer accepts as its input a set of colour photographs, rep-
187 resenting rectangular subareas of a cereal field, taken by a drone from above.
188 The task of the recognizer is to produce a set of detected sowing rows for each
189 image. Each row is represented by a sequence of line segments that together
190 constitute the row and visualized by overlaying the lines on the original image.
191 Another visualization to be used is to mark the adjacent rows with different
192 colours. Joining the neighbouring, partially overlapping images together is a
193 different type of problem and not discussed here.

194 *4.1. Segmentation*

195 Recognition of plants from raw data may be problematic without preprocess-
196 ing. Young plants, being our main interest here, are small and can be difficult to
197 separate from a dominating background, especially on a sunny weather (see Fig.
198 3a). In this figure, the actual sowing rows are straight but the sowing machine
199 was turned at the site after sowing, and the back rake of the machine made the
200 curved furrows.

201 The segmentation of the plant objects is attempted here by two alternative
202 algorithms: k-means clustering of image elements (Lloyd, 1982), and a *colour*
203 *channel transform* combined with Otsu's method. In order to make the work
204 more self-contained, we will briefly recall their main ideas below.

205 *k-means clustering of image elements*

In general, the k-means clustering algorithm obtains a data set X of n objects $x_j (j = 1, \dots, n)$, where $x_j = (x_{j1}, x_{j2}, \dots, x_{jr})$, for a fixed dimension $r \geq 1$. The aim of the clustering is to search, for a given k , a partition $C^* = (C_1^*, C_2^*, \dots, C_k^*)$ such that

$$C^* = \operatorname{argmin}_C \sum_{i=1}^k \sum_{x \in C_i} \|x - \mu_i\|^2 \quad (2)$$

206 where C stands for all possible partitions of X , and μ_i the center point of the
 207 objects $x \in C_i$. The ' $\|\cdot\|$ ' operator stands for the vector norm which is here
 208 assumed to be simply the Euclidean distance (the L_2 norm). In other words,
 209 one wants to find a set of k disjoint clusters covering all the objects in X such
 210 that the sum of intra-cluster distances from the cluster center points is minimal.

211 We notice that k-means clustering can be applied in a natural way to a
 212 colour image of $n = N \times M$ pixels in the *CIE colour space*. The data set
 213 $X = [x_1, x_2, \dots, x_n]^T$, where each $x_i \in X$, is a two-dimensional vector containing
 214 the values of colour channels a_i^* and b_i^* of pixel i . (Intensity channel L^* is omitted
 215 here, due to changing lighting conditions.) When choosing $k = 3$, the clusters
 216 of C^* stand for C_R , C_G , and C_B (closest to red, green, and blue, respectively).
 217 In row recognition, cluster C_G should stand for plant pixels (see Fig. 3b).

218 The method gave good results for our data, but as a drawback the execu-
 219 tion times are long because of the inherent NP-hardness of the problem (see
 220 Appendix, Table 3).

221 *Gray-scale transform and binarization with Otsu's method*

It is typical of the previous plant row recognizers that individual plants have been found by some kind of transformation of colours into gray-scale values. This can be done by enhancing the values of the green channel, and at the same time reducing those of blue and red (see Jiang et al. 2015, Woebbecke et al. 1995, and Motohka et al. 2010). In the present work we apply the vegetation index I_H discussed by Burgos-Artizzu et al. (2011):

$$I_H(x, y) = I_g(x, y) \times 1.262 - I_r(x, y) \times 0.884 - I_b(x, y) \times 0.311, \quad (3)$$

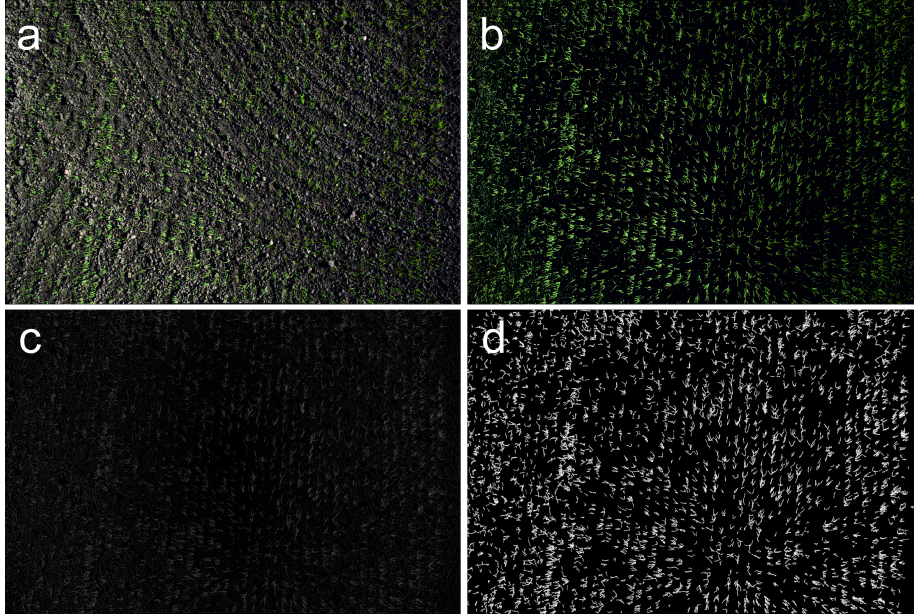


Figure 3: a) A sample colour photo of young plants, without preprocessing. b) The effect of k-means clustering to Fig. 3a. The pixels of the C_G -cluster are shown. c) The effect of the vegetation index transform for Fig. 3a, converted to gray-scale. d) The result of preprocessing Fig. 3a by using the vegetation index, thresholding by Otsu's method, and filtering off small connected components.

222 where (x, y) stands for a pixel in an $M \times N$ image I (see Fig. 3c, for an example).

223 The transform clearly works in $O(M \times N)$ time.

A gray-scale image I_H can be transformed into a binary image by the mapping (Gonzalez and Woods 2002)

$$I_B(x, y) = \begin{cases} 1, & \text{if } I_H(x, y) > t \\ 0, & \text{if } I_H(x, y) \leq t \end{cases} \quad (4)$$

Threshold t is selected to minimize the weighted sum of the internal variances of the pixel values in the 0-pixel and 1-pixel groups Otsu (1975):

$$\sigma_w^2(t) = \omega_0(t)\sigma_0^2(t) + \omega_1(t)\sigma_1^2(t), \quad (5)$$

224 where $\sigma_0^2(t)$ is the variance of gray-scale values less than or equal to the threshold

225 t ; these pixels are thus changed to 0-bits. Similarly $\sigma_1^2(t)$ is the variance of the

226 gray-scale values greater than t . Further, the term $\omega_0(t)$ is the total number of
 227 0-bits, and $\omega_1(t)$ is the total number of 1-bits, for a given t .

228 In the last step we remove small binary fragmentary objects that can be
 229 considered noise. This is done by expressing the 0/1 image as an undirected
 230 graph G of $M \times N$ nodes $V = \{(x, y)\}$ where the nodes stand for the pixels of
 231 the image $I_B(x, y)$. There is an arc in G between node (x, y) and each of its
 232 eight neighbours $((x - 1, y - 1), (x, y - 1), \dots, (x + 1, y + 1))$ if both (x, y) and
 233 its neighbour contain a 1-bit (Bai et al. 2012). Then we define the connected
 234 components of G by a fast algorithm and filter out those components which
 235 include less than a given limit t_{cc} of nodes. This process changes $I_B(x, y)$ into a
 236 filtered image $I'_B(x, y)$. The value of t_{cc} naturally depends on the application. In
 237 our data, manual inspection of a sample gave the average plant size of somewhat
 238 over 160 pixels. In Fig. 3d, the connected components with less than 50 pixels
 239 have been filtered out. The value of parameter t_{cc} should be derived from the
 240 training data of the plant row recognition system.

241 4.2. Feature extraction

In the previous section the plants were separated from the background. Now we introduce features which will be used for automatic determining of the number of sowing rows, and mapping of plants to their rows. For doing this, consider a connected component i . We determine the point of gravity (\bar{x}_i, \bar{y}_i) of i , and the angle θ of the straight line approximating the sowing row. The angle will be found from the largest coefficients of the *discrete Fourier transform* of the binary image I'_B , from which the smallest factors have been removed (see e.g. Cormen et al. 2001, Chapter 30). The feature to be determined is simply the x -coordinate of the component's point of gravity in a transformed space, obtained as follows.

$$\bar{x}'_i = [(\bar{x}_i - N/2)(\bar{y}_i - M/2)] \begin{bmatrix} \cos \theta & -\sin \theta \\ \sin \theta & \cos \theta \end{bmatrix} + N/2 \quad (6)$$

242 *Center of gravity*

Consider a connected component R_i in the filtered binary image I'_B . The geometric center of gravity of R_i is then (\bar{x}_i, \bar{y}_i)

$$\bar{x}_i = \sum_{(x,y) \in R_i} (x/|R_i|) \text{ and } \bar{y}_i = \sum_{(x,y) \in R_i} (y/|R_i|), \quad (7)$$

243 where $|R_i|$ is the number of pixels in R_i .

244 *Directional angle θ of the rows*

245 The Fourier transform can be used to convert a signal into a sum of sine and
 246 cosine functions. The transform is useful in image applications because the low
 247 frequency coefficients of the transformed signal correspond to the main features
 248 of the original signal in spatial space.

249 A binary image I'_B can be transformed by the two-dimensional discrete
 250 Fourier transform to the form

$$I_F(k, l) = \sum_{m=1}^M \sum_{n=1}^N I'_B(m, n) e^{-j2\pi km/M} e^{-j2\pi ln/N}, \quad (8)$$

251 where $j = \sqrt{-1}$, $k = 1, 2, \dots, M$, and $l = 1, 2, \dots, N$. The result can be inter-
 252 preted as a matrix (or image in the frequency space) where the *DC*-coefficient
 253 (called 0-frequency) with indexes $(1, 1)$ is in the left-upper corner. For the needs
 254 of interpreting the direction of the sowing rows, the frequency space is shifted so
 255 that the 0-frequency is in the middle of the coordinate space, as shown in Fig.
 256 4. This rearranged transformed "image" is called the I_C image of the original
 257 spatial binary image.

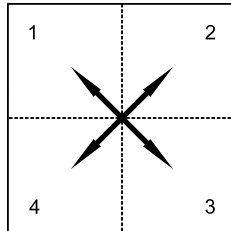


Figure 4: Centering the 0-frequency by interchanging the quadrants $1 \leftrightarrow 3$ and $2 \leftrightarrow 4$.

258 Fig. 5 shows a 3-dimensional I_C view of a typical image in our application.
 259 The coefficients for low-frequency functions are in the middle (marked by yellow)
 260 in this view. The high peaks close to the 0-frequency peak contain information
 261 about the direction of the regularly repeating patterns (here for the parallel,
 262 equi-distant sowing rows) in the original image. Note here that the "peaks" in
 263 I_C consist of several high coefficient values around the absolute maximum.

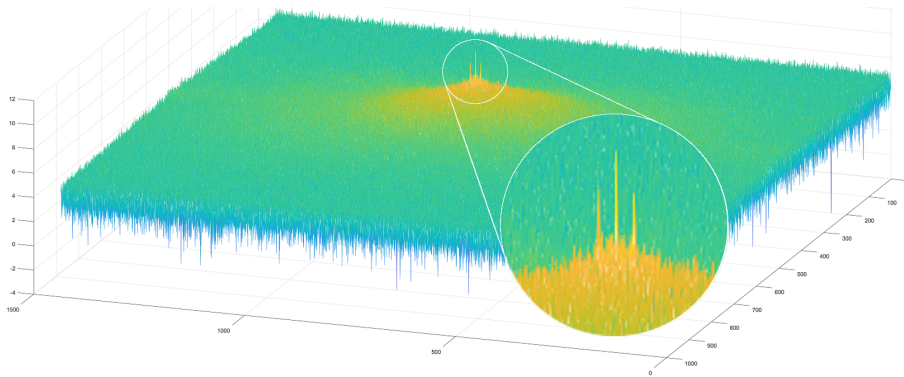


Figure 5: 3D view of the Fourier transform.

264 For automatic extraction of the peaks, image I_C is filtered twice. First,
 265 the 0-frequency peak is removed by setting the 6×6 square in the middle of
 266 I_C to zeroes (experimental choice). This gives us a coefficient matrix I_{-DC} .
 267 Secondly, we want to find a small number of the highest remaining peaks from
 268 I_{-DC} . It turns out that when the plant rows are not extremely sparse, two
 269 peaks suffice (actually one because the transform is symmetric with respect to
 270 the origin). Nevertheless, the algorithm works well for other settings, too, up to
 271 10 peaks. The search for the highest peaks will be done by thresholding I_{-DC}
 272 with different increasing threshold values, denoted p , and iteratively searching
 273 for the largest p -value which yields the wanted number of peaks¹, which form
 274 the basis for a good estimate of the required rotation angle. In fact, a regression
 275 line through the peaks should be perpendicular to the direction of rows. The

¹Plain sorting of the elements of I_F would be the other option, but thresholding is easier when looking for connected clusters of low-frequency values.

276 thresholding produces a binary matrix $I_T^*(x, y)$ of size $M \times N$, where the peaks
 277 appear as 1-bits, others being zeroes.

278 Josso et al. (2005) have shown how the *principal component analysis (PCA)*
 279 can be applied to estimate the texture orientation of an image, on the basis of
 280 high peaks of the Fourier transform. Here we apply their method for finding
 281 the angle of the sowing rows, with respect to the basic direction determined by
 282 the camera position.

283 For the needs of PCA, let $X_T = (x_1, x_2, \dots, x_q)$ and $Y_T = (y_1, y_2, \dots, y_q)$
 284 give the (x, y) -coordinates of the 1-pixels in the thresholded binary image I_T .
 285 Calculate the *covariance matrix*

$$\Sigma = \begin{bmatrix} \sigma(X_T, X_T) & \sigma(X_T, Y_T) \\ \sigma(Y_T, X_T) & \sigma(Y_T, Y_T) \end{bmatrix} \quad (9)$$

where

$$\begin{aligned} \sigma(X_T, X_T) &= E[(X_T - E(X_T))(X_T - E(X_T))] = \frac{1}{q-1} \sum_{i=1}^q (x_i - E(X_T))^2 \\ \sigma(Y_T, Y_T) &= E[(Y_T - E(Y_T))(Y_T - E(Y_T))] = \frac{1}{q-1} \sum_{i=1}^q (y_i - E(Y_T))^2 \\ \sigma(X_T, Y_T) &= \sigma(Y_T, X_T) = E[(X_T - E(X_T))(Y_T - E(Y_T))] \end{aligned}$$

The largest eigenvectors of the covariance matrix Σ point to the directions of the (x, y) -space containing the biggest amount of variance. The eigenvectors $\bar{v} \in R^2$ ($\bar{v} \neq 0$) and eigenvalues λ fulfill the equality $\Sigma \bar{v} = \lambda \bar{v}$, and the principal component of this vector equation is

$$v_1 = \operatorname{argmax}_{\|v\|=1} \{ \bar{v}^T \Sigma \bar{v} \}, \quad (10)$$

where $v_1 = (v_y, v_x)$ is the eigenvector corresponding to the largest eigenvalue λ_1 . Since we are dealing with frequency peaks of the Fourier transform, the eigenvector is perpendicular to the plant rows. The wanted general angle of the sowing rows is then

$$\theta = -(\operatorname{atan2}(v_y, v_x)), \quad (11)$$

286 where $\text{atan2}(x, y)$ is the angle between the positive x -axis and the ray to the
 287 point (x, y) .

288 *4.3. Unsupervised learning step*

After the feature extraction, the next step is to map plants to their rows. The purpose is to split a data set \bar{X}' containing n plant positions \bar{x}' into clusters $K = \{K_1, K_2, \dots, K_k\}$ where k is the number of rows. Here we use *k-medoids*, a classical partitioning method which seeks for k "representative entities" that minimize the overall dissimilarity of every entity of the data set to the nearest representative entity (Kaufman and Rousseeuw, 1987). We define a cluster as the set of entities which have been assigned to the same representative entity. Clusters are derived from decision variables y_i and z_{ij} with the following optimization model:

$$\text{minimize } \sum_{i=1}^n \sum_{j=1}^n \|\bar{x}'_i - \bar{x}'_j\|^2 z_{ij} \quad (12)$$

subject to

$$\sum_{j=1}^n z_{ij} = 1, j = 1, 2, \dots, n \quad (13)$$

$$z_{ij} \leq y_i, i, j = 1, 2, \dots, n \quad (14)$$

$$\sum_{i=1}^n y_i = k, k = \text{number of clusters} \quad (15)$$

$$y_i, z_{ij} \in \{0, 1\}, i, j = 1, 2, \dots, n \quad (16)$$

289 where y_i is equal to one if and only if \bar{x}'_i is assigned as a representative entity
 290 and z_{ij} is equal to one if and only if \bar{x}'_j is selected to the cluster of which \bar{x}'_i is the
 291 representative entity (Kaufman and Rousseeuw, 1987). K-medoids requires the
 292 number of clusters to be pre-specified. Therefore, the next phase is to determine
 293 the number of sowing rows in a an image.

294 *Number of rows*

Locations of the sowing rows are relocated in the spatial image by a brute force technique where the binary image $I_B(x, y)$ is rotated counter-clockwise by

the angle $\pi - \theta$, so that the rows turn vertical with respect to the x -coordinate axis. Denote the rotated image by I_R . All pixel positions in the x -axis from x_1 to x_n are then considered, and the number of corresponding 1-bits in each column is calculated:

$$S(x_i) = \sum_{y=1}^M I_R(x_i, y) \quad (17)$$

The idea is to find the x -ranges that contain a lot of 1-pixels, and in this way to locate the sowing rows. While doing this, one may filter out some fragmentary 1-pixel objects by the median filter

$$S_{med}(x_i) = \text{med}(S(x_i - \omega), S(x_i - \omega + 1), \dots, S(x_i + \omega)), \quad (18)$$

where ω is a user-defined parameter (see Huang et al. 1979). In our application, values of ω from the range 1 to 15 worked well. Suppose that x^* is a local maximum point for $S(x_i)$. It is then accepted as a center point of a sowing row if there is no larger median within any interval $(x - \omega, \dots, x + \omega)$ for $x \in [x - \epsilon, x + \epsilon]$, and if $S(x^*)$ is not smaller than a threshold ζ :

$$(S_{med}(x^*) \geq S_{med}(x)) \text{ and } (S(x^*) \geq \zeta) \quad (19)$$

295 for $|x - x^*| \leq \epsilon$. Parameter ζ is a predefined constant, representing the minimum
 296 accepted number of green pixels in a pixel column. The experimentally obtained
 297 values $\zeta = 20$ and $\epsilon = 75$ were applied. The number k of sowing rows is now
 298 the number of local maximum points (x^*) found in the above process, i.e. if
 299 $X^* = \{x_1^*, x_2^*, \dots, x_k^*\}$, then $k = |X^*|$, see Fig. 6, for an example.

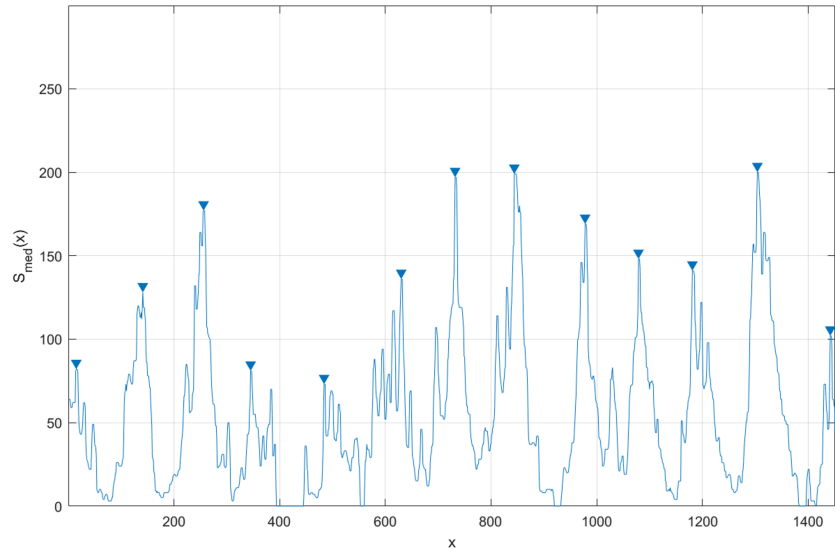


Figure 6: Finding frequency peaks after rotating the sowing rows to vertical.

300 *Linear regression*

301 The result of assigning the points of gravity to the approximated rows makes
 302 the estimation of the sowing rows possible. We therefore estimate the coefficients
 303 α and β of the straight lines $(x, y) = (\alpha + \beta y, y)$ by means of the least squares
 304 method (see Fig. 7).

305 Note that after applying the least squares method, the lines describing the
 306 sowing rows may not be exactly parallel because the center of weight of a plant
 307 is not identical with the position of the seed and because seeds may slightly
 308 move during sowing from the theoretical position of the sowing row.

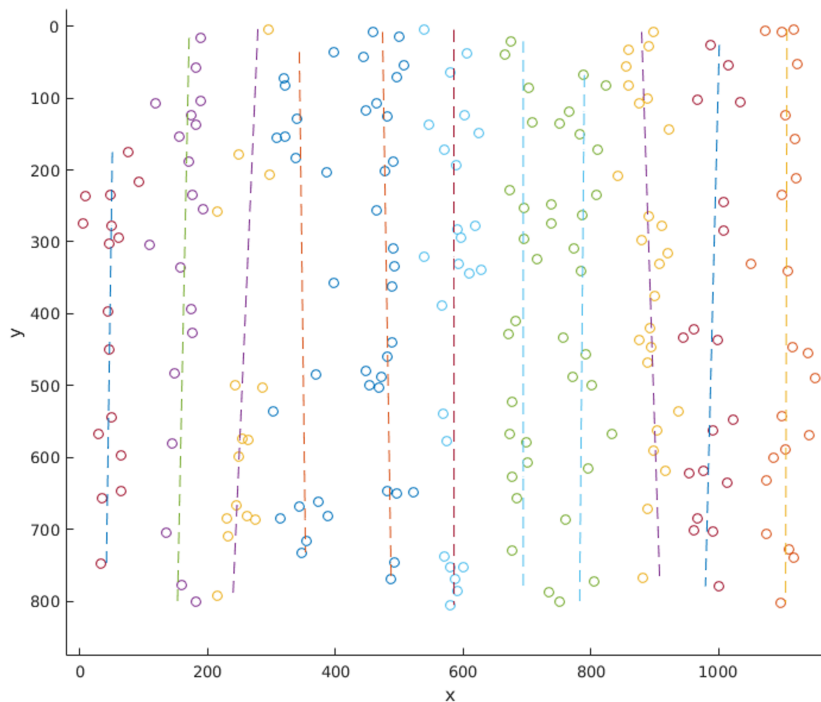


Figure 7: Sowing rows obtained with the least-squares method.

309 **5. Test results**

310 The method of Section 4 was tested with a set of 48 aerial photographs
 311 taken by a drone from an altitude of approximately 10 meters above a rye field,
 312 in South-Western Finland in fall 2015. The rye (cv. Evola) had been sown
 313 25.8.2015, and the plants were 16 days old when photographed. The sowing
 314 machine (Väderstad Rapid) used a 12-cm row-to-row distance. All photography
 315 was done in the morning, between 8:50 and 9:30 o'clock. The weather was clear
 316 and the solar elevation was approximately 25° . There were no weeds on the
 317 field. The camera used was Canon EOS 5D Mark 3, with resolution 5808×3876
 318 pixels, and the images were converted to the TIFF format before use. The
 319 direction of shooting was straight down from the drone. The vertical axis of
 320 the 2D-images was roughly parallel with the sowing rows, so that the required
 321 rotation angles were usually rather small.

322 In order to reduce the effect of perspective distortion, the images were par-
323 titioned into 4×4 subimages of size 1452×969 pixels, and the subimages were
324 processed separately.

325 Manual evaluation of the segmentation step revealed that the excess green
326 with Otsu thresholding performs fairly well in most pictures, although 11.5-25.2
327 % of the connected components contained also soil pixels in the five images
328 analyzed manually (Table 1). In 3.3-13.9 % of the connected components, one
329 plant was split to more than one component, and 13.8-28.5 % of the connected
330 components contained pixels from more than one plant. 0.7 to 26.8 % of the
331 connected components, depending on the image, contained no plant pixels at all.
332 In overall, 68.8-92.4 % of plants in the photographs were successfully included
333 in the connected components.

334 The errors made by the segmentation suggest that soil has excessively green
335 pixels that are taken as plants by the method. Examination of the distributions
336 of red, green and blue colors in the connected components shows that their
337 intensity distributions may be quite similar (Images 3 and 4 in Fig. 8). However,
338 this does not seem to correlate with errors in segmentation, as the intensity
339 distributions suggest that Image 2 should become well segmented, but in the
340 segmentation it has the lowest quality of the inspected five images (Table 1).
341 Often the soil pixels that became segmented as plant material were located on
342 the side of an earth particle and formed a longish, somewhat leaf-like form in
343 the final segmented picture.

Table 1: Evaluation of the segmentation step. Percentages (actual numbers in parenthesis) of connected components that contained only one plant (Good components), some of them also containing soil pixels; cases where a plant is split to separate components (Split plants); connected components that contained more than one plant (Multiple plants) and connected components that did not contain plant pixels (No plants). The (%) of plant pixels in connected components lists manual estimations of $100 \times (\text{plant pixels in connected components}) / (\text{all plant pixels in the image})$. The last column shows the percentages of manually estimated soil pixels in connected components. The contents were calculated by manual examination of images 2, 3, 4, 14 and 35.

Image nr	Good components		Split plants	Multiple plants	No plants	(% of plant pixels in connected components)	(% of soil pixels in connected components)
	Only plant pixels	Also soil pixels					
2	43.7(80)	11.5(21)	3.3(6)	14.8(27)	26.8(49)	68.8	28.5
3	41(59)	16.7(24)	7.6(11)	20.8(30)	13.9(20)	85.5	19.3
4	30.6(45)	25.2(37)	12.9(19)	23.8(35)	7.5(11)	86.4	9.3
14	42.4(61)	14.6(21)	13.9(20)	28.5(41)	0.7(1)	88.6	4.8
35	37.3(47)	23(29)	8.7(11)	20.6(26)	10.3(13)	92.4	14.9

344 The errors made by the row recognizer were analysed manually (Table 2).
345 The accuracy of the method was calculated as the ratio of correctly classified
346 plant areas (= connected components) to the total number of plant areas. Here,
347 the plant area was defined as the area classified as plant material by the seg-
348 mentation algorithm. To aid the manual evaluation we utilized the Matlab
349 Image Region Analyzer tool. The row recognizer was developed using Matlab
350 programming language, and the execution times were measured by a PC (Intel
351 Core i7 @ 8×3.6 GHz, 16 GB RAM) using Ubuntu 18.04 operating system. For
352 practical reasons, the observed times do not include the k-means segmentation,
353 nor the estimation of regression lines.

354 Fig. 9 represents a typical aerial photo from a field soon after sowing, coupled
355 with an illustration of obtained results. The classification of individual plants
356 into rows is indicated by using different colours.

357 Fig. 10 is somewhat similar, but contains rather dense groups of plants,
358 affecting a bit the clustering of green pixels into distinct plants. A couple of

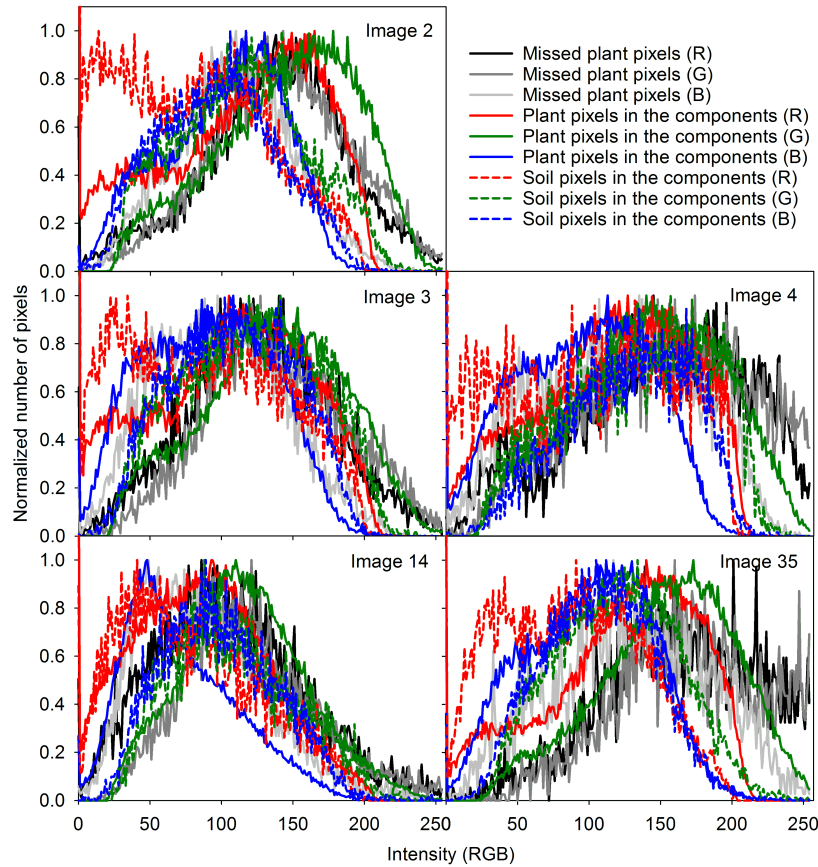


Figure 8: Distribution of red, green and blue in connected components (colored lines) and in the plant pixels not present in the components (back and gray lines) in five images. Pixels were manually classified as plant (solid lines) or soil (dashed lines).

359 connected components are too large, but otherwise the row detection succeeds.
 360 Some non-germinated spots can be observed, but these gaps do not essentially
 361 disturb the detection of rows.

362 Since the compass direction of the drone camera followed rather closely to the
 363 moving direction of the sowing machine, the rotations required to make the rows
 364 vertical were rather small. Figs. 11 and 12 were manually rotated 90 degrees
 365 in order to test the determination of the skewness of rows. The former image
 366 was an easier case, with rather smooth distribution of plants. The obtained

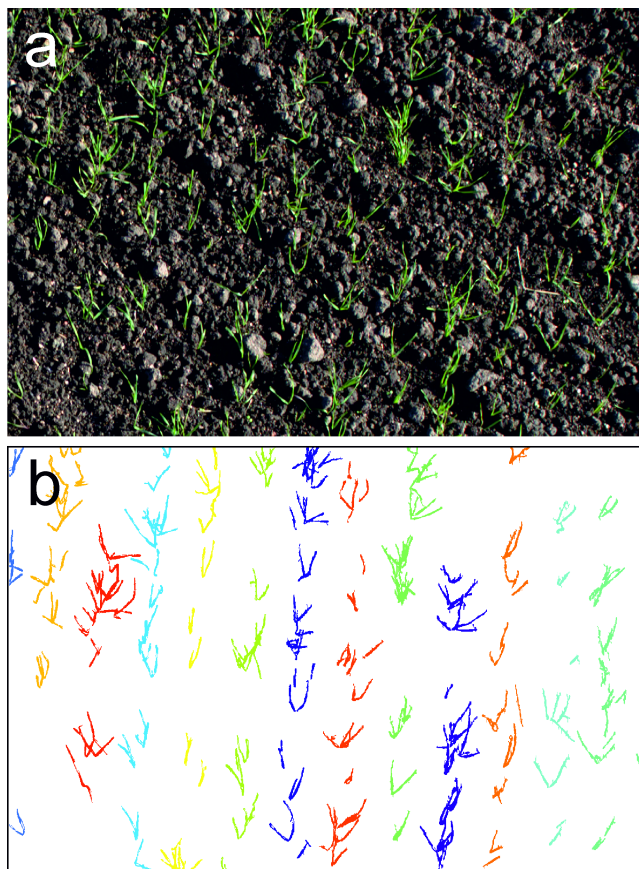


Figure 9: Test result for image 44.

367 classification into rows is quite close to what a human viewer would expect.
368 The latter (Fig. 12) was a hard case, with large gaps but also quite dense spots.
369 The result is basically acceptable, although some choices can be questioned.
370 In fact, even for a human annotator it would be difficult to decide the correct
371 classification, without knowing the larger context. It must be emphasized that
372 the most of our images were easier to analyze, than these two cases.

373 On the basis of a qualitative inspection of row visualizations, it is justified
374 to claim that the clustering of plants into rows in most cases matches with the
375 decisions made by a human analyst. More detailed results concerning automatic
376 versus manual classification are given in the appendix. The combined result of

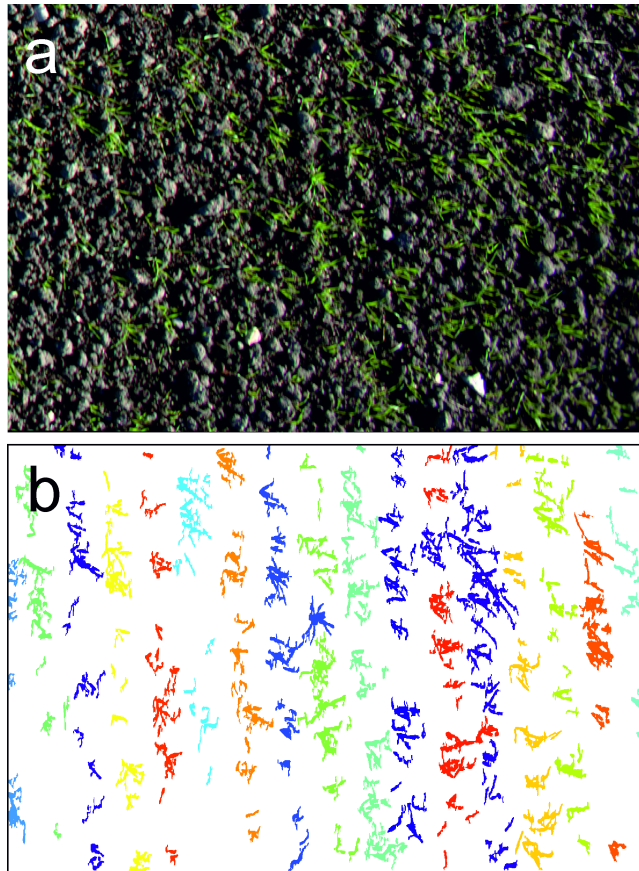


Figure 10: Test result for image 32.

377 manually checking all sowing row candidates in each test image was that about
378 94 per cent of the plants were classified into correct rows, on the average.

379 The processing time of a single 1452×969 image was about 0.11 seconds
380 by our (non-optimized) implementation. After further refinement, we expect to
381 still improve both the accuracy and the speed of the tool.

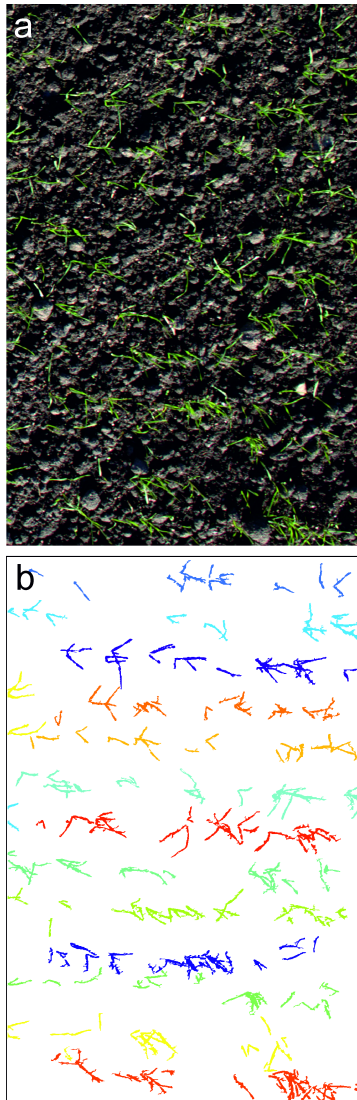


Figure 11: Test result for image 43.

Table 2: A summary of automatic versus manual analysis of sowing rows for n=48 test images. "Plants" refers to all components classified as plants by the segmentation algorithm.

	Predicted nr of rows	True nr of rows	Plants classified into wrong rows	Total no of plants	Classification accuracy(%)	Execution time (sec)
Mean	13.958	14.5	9.958	165.375	94.195	0.111
Median	14	14.5	7.5	153	94.895	0.112
SD	1.687	1.81	7.997	41.535	4.066	0.014

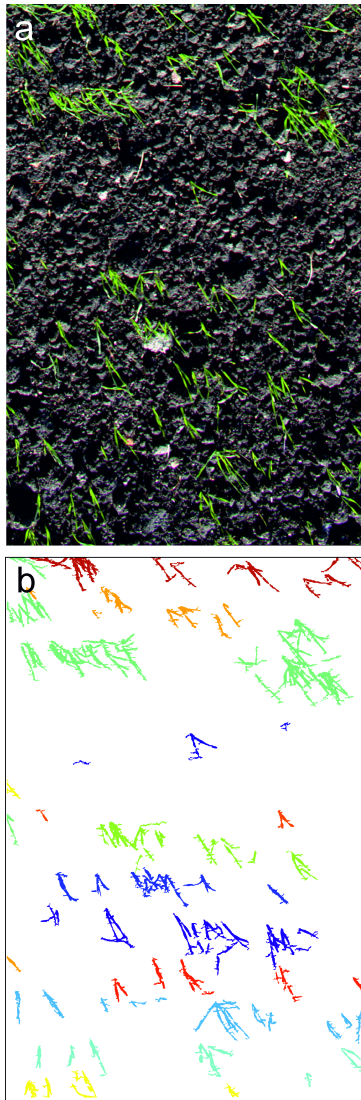


Figure 12: Test result for image 39.

382 6. Discussion

383 The results clearly show that the proposed method is capable of recognizing
384 sparsely growing plants sown row-wise. In addition, the direction of the rows
385 may vary to a certain extent. Also, the method makes a reliable calculation
386 of the number of rows. Actually, the results are surprisingly good, taking into

387 account that the method uses basically only one geometric feature (center of
388 gravity for the connected components) in classification. It turned out that
389 the recognition of horizontal rows was somewhat harder than that of vertically
390 oriented rows (due to infinite tangent of the perpendicular direction). This is
391 easily taken care of by studying also the 90 degrees rotated photo.

392 The finding that the segmentation of plants with the excess green method
393 and Otsu thresholding sometimes makes errors may suggest that the soil may
394 contain truly excessively green pixels, at least when photographed from an UAV
395 early in the morning when the sun is still low in the sky.

396 While the running time is on an acceptable level (at least for off-line process-
397 ing), the current implementation leaves plenty of possibilities for speeding up,
398 concerning both algorithms and the choice of the programming environment.
399 There are several ways to enhance the efficiency of the recognizer. For example,
400 the usage of a graphics processing unit would surely be of help. Another way
401 would be rethinking of program loops by vectorization techniques.

402 The present study was limited to finding nearly parallel, roughly straight
403 rows of plants, occurring in a window of restricted size. In particular, we made
404 a restriction that the studied image is fully inside a single driving lane of the sow-
405 ing machine. Handling of images covering the border area of two lanes requires
406 a generalization. The simplest solution is to view the image as a combination of
407 two subsets of parallel rows with the same inter-row distance, but with different
408 offsets. In the frequency domain we would say that the dominating frequencies
409 are divided to two phases. If the lanes are parallel, the rows can be rotated to
410 vertical even in this case. If the lanes overlap, the border area would consist of
411 alternating intervals of two sizes between the peaks of local maxima. If there is
412 no overlap, a single arbitrary-size interval occurs between the lanes. We leave
413 the detailed study of this generalization for future work.

414 In the present study, all plants were classified to belong to a row. The next
415 step of the study would be to find and mark the weed candidates on the images
416 automatically, coupled with their coordinates. The suspected weeds are plants
417 growing in between the sowing rows, i.e. far from the line defining the row.

418 Assuming that sufficiently precise locations are known and marked on a map of
419 the field, the farmer is able to remove the harmful plants.

420 **Acknowledgement**

421 This study was financially supported by European Agricultural Fund for Ru-
422 ral Development (grant nr. 30934), Academy of Finland (grant nr. 307335), Uni-
423 versity of Turku Graduate School, Turku University Foundation, and Väisälä Fund.

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516 tering algorithm and shortest path method. *Computers and Electronics in
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Table 3: Processing time of segmentation methods over different resolution images.

Image resolution	Average execution time (sec)	
	K-means	Colour channel transform combined with Otsu's method
1452 x 969	12.225	0.041
5808 x 3876	160.931	0.867

Table 4: Automatic versus manual analysis of sowing rows.

Image nr	Predicted nr of rows	True nr of rows	Incorrectly classified plants	Total nr of plants	Classification accuracy (%)	Execution time (sec)
1	16	16	30	191	84.29	0.119
2	15	15	4	170	97.64	0.113
3	15	16	9	147	93.87	0.115
4	14	14	5	124	95.96	0.112
5	13	16	24	191	87.43	0.110
6	14	15	10	188	95.21	0.114
7	15	15	1	160	99.37	0.114
8	15	15	4	176	97.72	0.118
9	15	15	2	156	98.71	0.111
10	15	15	3	133	97.74	0.101
11	14	15	4	153	97.38	0.092
12	14	14	1	149	99.32	0.095
13	15	15	2	132	98.48	0.094
14	14	14	3	153	98.03	0.109
15	14	14	7	158	95.56	0.094
16	13	13	4	151	97.35	0.094
17	13	14	18	211	91.46	0.110
18	13	13	10	187	94.65	0.108
19	14	15	10	158	93.67	0.112
20	14	14	4	120	96.66	0.105

Table 4: Automatic versus manual analysis of sowing rows.

Image nr	Predicted nr of rows	True nr of rows	Incorrectly classified plants	Total nr of plants	Classification accuracy (%)	Execution time (sec)
21	16	16	17	267	93.63	0.141
22	15	16	6	266	97.74	0.124
23	13	15	23	147	84.35	0.102
24	16	16	12	219	94.52	0.121
25	15	17	22	194	88.65	0.124
26	18	18	3	151	98.01	0.113
27	15	18	21	228	90.78	0.126
28	15	16	22	229	90.39	0.121
29	17	18	7	175	96.00	0.115
30	16	16	10	206	95.14	0.119
31	15	17	29	227	87.22	0.122
32	17	17	4	249	98.39	0.123
33	15	14	22	202	89.1	0.137
34	13	14	24	176	86.36	0.146
35	13	14	10	126	92.06	0.117
36	13	13	7	116	93.96	0.129
37	12	13	12	120	90	0.102
38	11	12	15	151	90	0.110
39	12	12	8	96	91.66	0.117
40	13	14	6	108	94.44	0.095
41	13	13	8	137	94.16	0.122
42	12	12	7	150	95.33	0.108
43	12	13	9	139	93.52	0.119
44	13	13	2	114	98.24	0.097
45	11	12	5	131	96.18	0.087
46	11	11	0	135	100	0.088
47	13	13	8	132	93.93	0.085
48	10	10	4	139	97.12	0.088